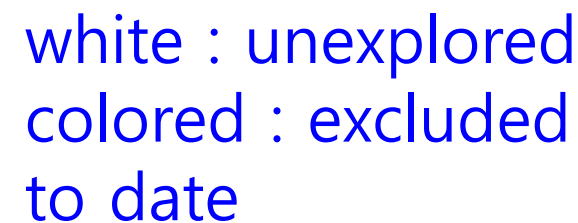


Microwave Cavity Axion Dark Matter Search

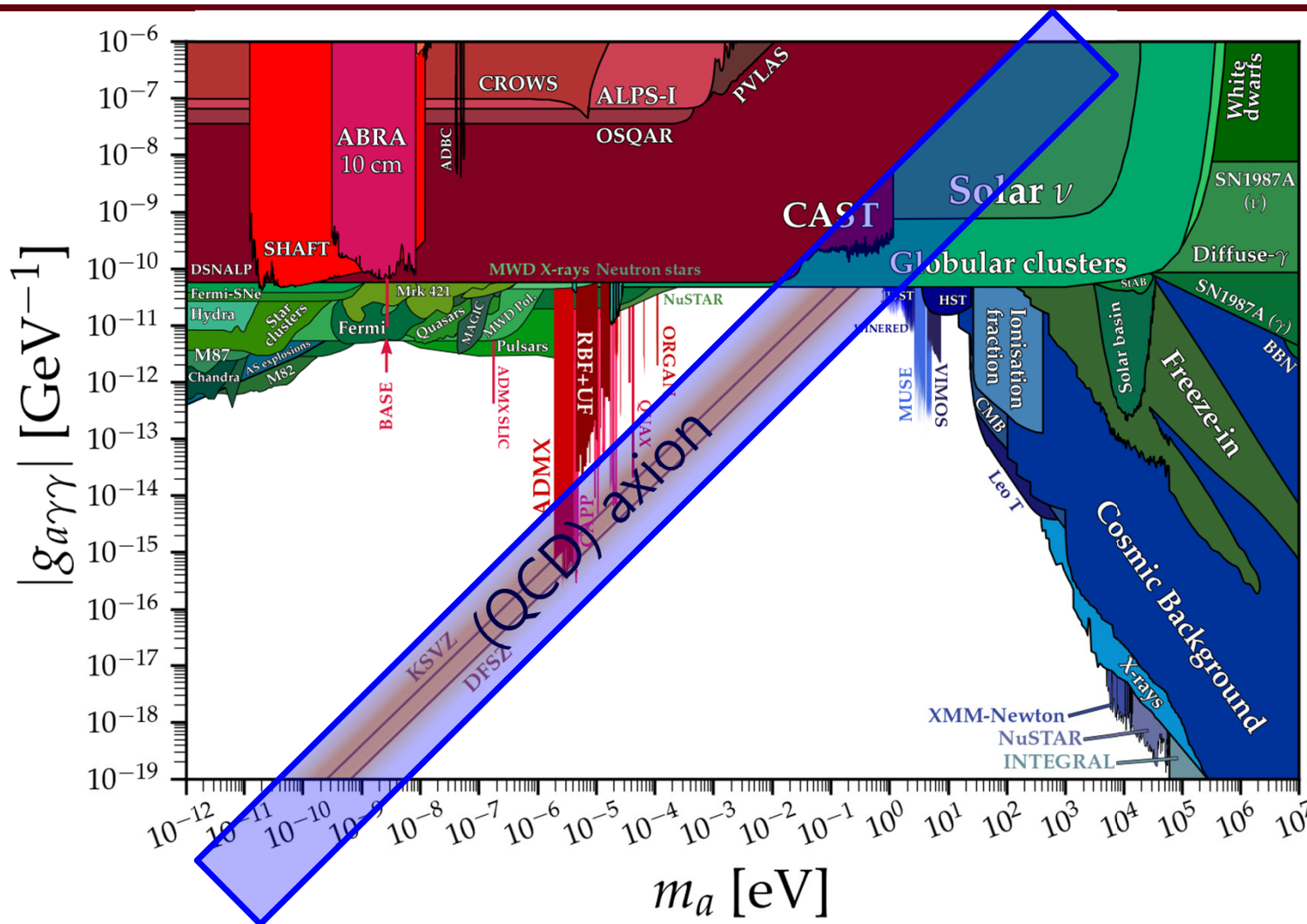
IHEP-KU workshop@KU, 2024 Oct. 14

Byeong Rok Ko

(Dept. of Accelerator Science, Korea Univ. Sejong Campus)

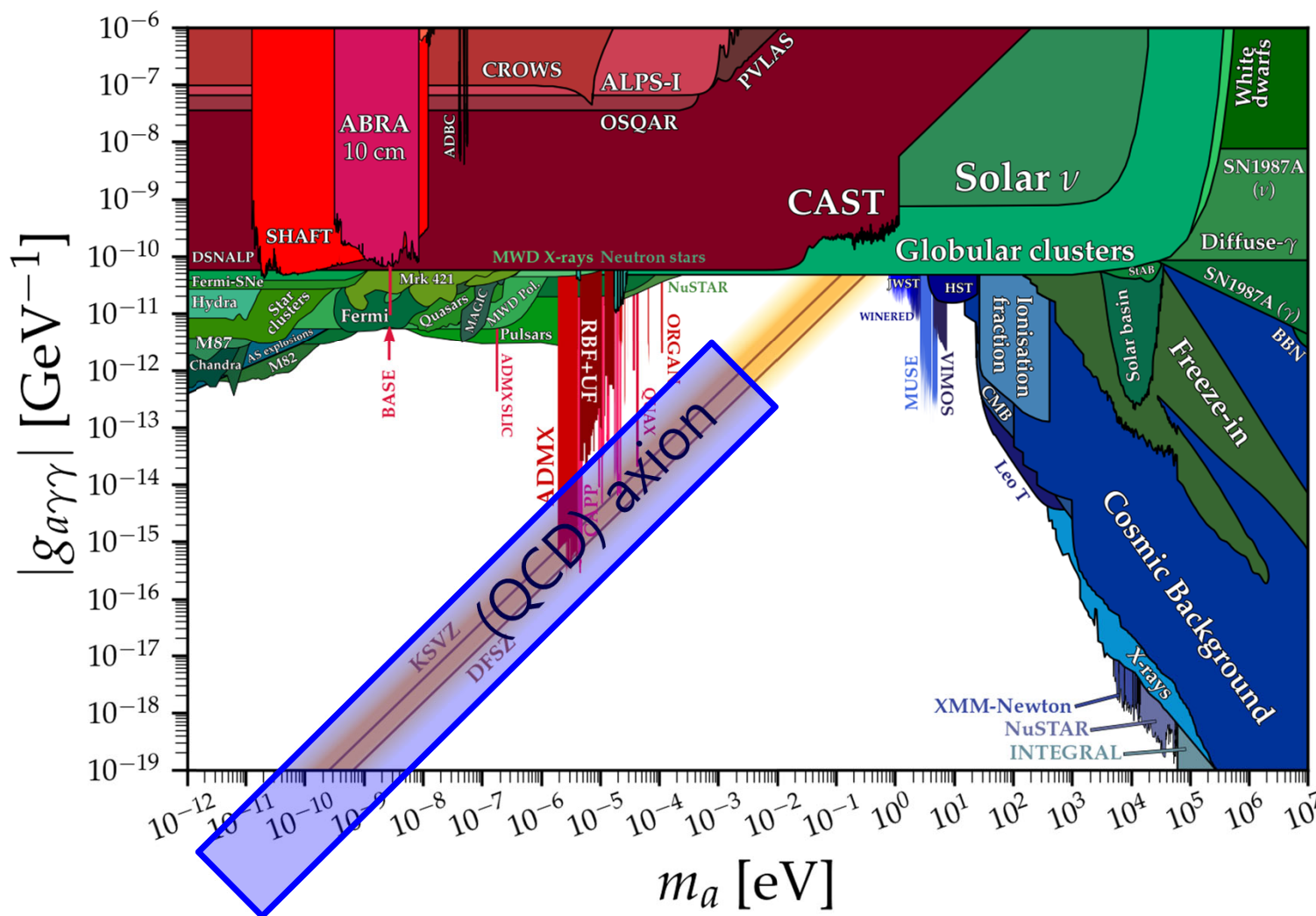


Axion dark matter search = Microwave cavity search



yellow band :
(QCD) axion,
a natural solution
of the strong CP
problem in the
Standard Model
(SM)

Axion dark matter search = Microwave cavity search



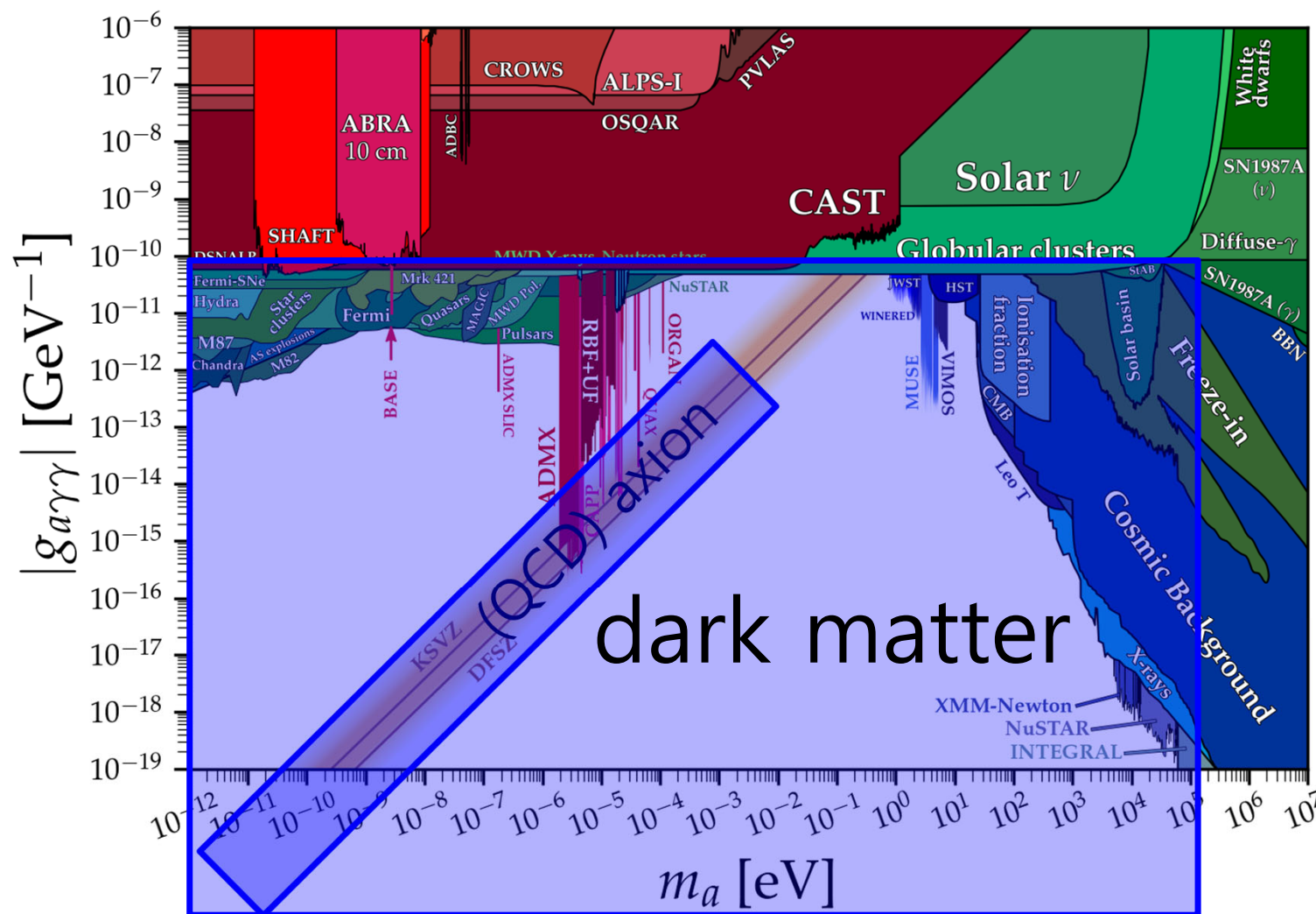
Upper limit by SN 1987A

Observation associated with neutrino events is consistent with the expectations assuming that the collapsed supernova core cools solely by neutrino emission.

If the core also cools by the axion emission, the neutrino burst is excessively reduced.

$$m_a < O(\text{meV})$$

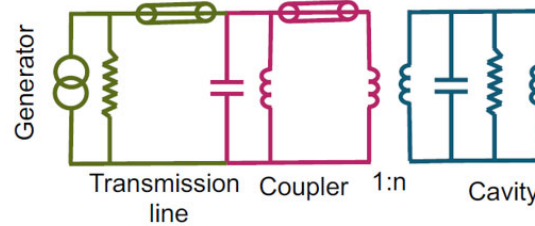
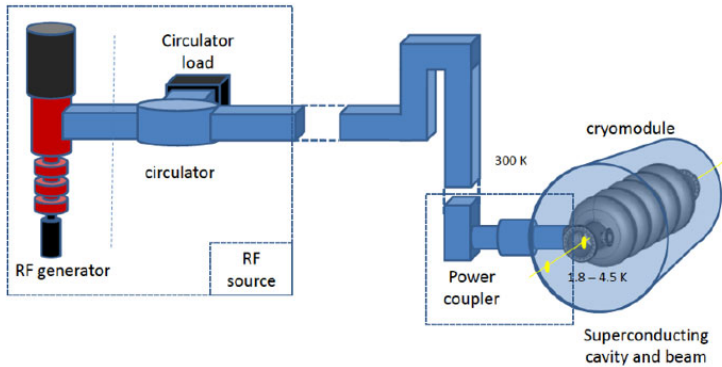
Axion dark matter search = Microwave cavity search



white : unexplored
as dark matter for
the coupling

They
(narrow spikes)
are all
employing a
microwave
cavity

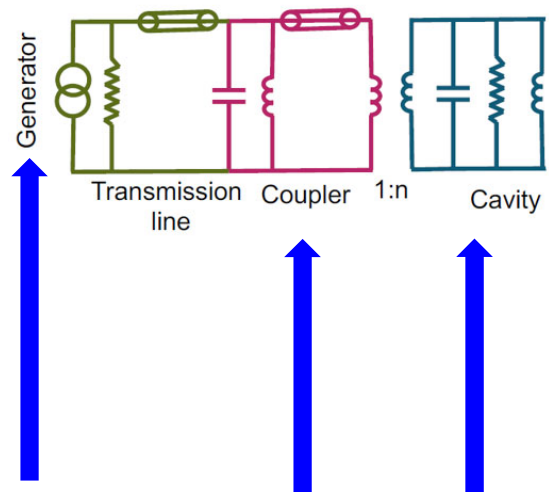
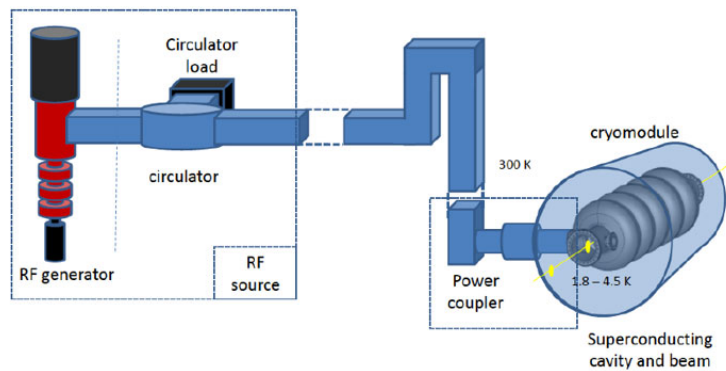
Microwave cavity is a crucial ingredient in accelerators and axion dark matter searches



accelerating gradient

$$E_{acc} \propto \sqrt{Q_{cavity}}$$

Microwave cavity is a crucial ingredient in accelerators and axion dark matter searches



axion dark
matter halo

$g_{a\gamma\gamma}$

cavity
mode

$E_a^{\alpha\gamma\gamma}$

accelerating gradient

$$E_{acc} \propto \sqrt{Q_{cavity}}$$

axion signal power

$$P_a^{\alpha\gamma\gamma} \propto Q_{cavity}$$

$$\rightarrow E_a^{\alpha\gamma\gamma} \propto \sqrt{Q_{cavity}}$$

$$\text{if } m_a = \nu_{cavity}$$



Axion as a solution of the Strong CP problem in the Standard Model

$U(1)_A$ problem

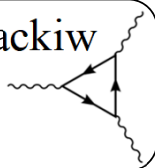
- S. Weinberg, $m_{\eta'} < \sqrt{3}m_\pi \sim 240$ MeV from the perturbed QCD, nominal $m_{\eta'} = 958$ MeV $>$ $m_p = 938$ MeV

Axion as a solution of the Strong CP problem in the Standard Model

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Adler-Bell-Jackiw
anomaly



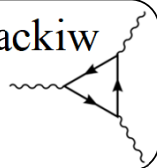
- G. 't Hooft, $U(1)_A$ is not a symmetry $\theta_{QCD} \frac{g^2}{32\pi^2} G_a^{\mu\nu} \tilde{G}_{\mu\nu a}$, succeeded to derive the nominal η' mass
- $\theta_{QCD} \frac{g^2}{32\pi^2} G_a^{\mu\nu} \tilde{G}_{\mu\nu a}$ is CP odd $\because G_a^{\mu\nu} \tilde{G}_{\mu\nu a} \sim \vec{E}^a \cdot \vec{B}^a$ and θ_{QCD} is a parameter,

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No neutron
electric dipole moment
(EDM)

- $d_n \sim \theta_{SM} \frac{m_u m_d}{m_u + m_d}$, $\theta_{SM} = \theta_{QCD} + \theta_{EW}$ with non-zero quark masses

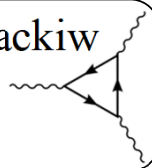
however, measured $\theta_{SM} \leq 10^{-10} \rightarrow$ very small, just putting θ_{SM} to 0 is not unnatural. The matter is zero θ_{SM} means CP is a good symmetry in the SM, but now know CPV in the kaon and B systems, and that in the kaon system at the time \rightarrow unnatural cancellation in θ_{QCD} & $\theta_{EW} \rightarrow$ Strong CP problem in the SM

Axion as a solution of the Strong CP problem in the Standard Model

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θ_{SM} promoted to
a dynamic variable

$$\theta_{SM} \rightarrow \theta_{SM} + \frac{a}{f_a}$$

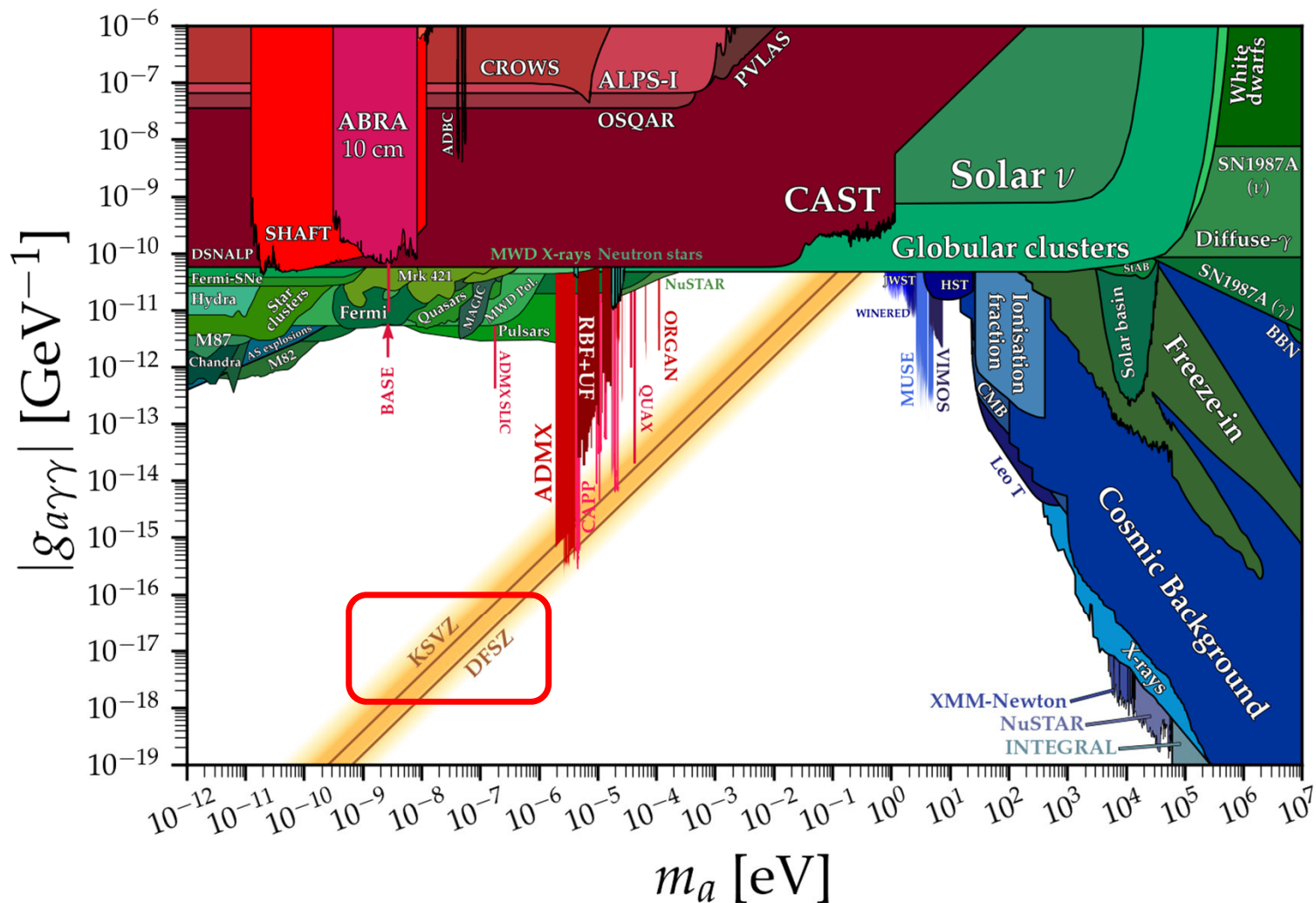
- by Peccei and Quinn (PQ), $\frac{g^2}{32\pi^2} \theta_{SM} G_a^{\mu\nu} \tilde{G}_{\mu\nu a} \rightarrow \frac{g^2}{32\pi^2} \left(\theta_{SM} + \frac{a}{f_a} \right) G_a^{\mu\nu} \tilde{G}_{\mu\nu a}$

f_a is the axion decay constant $\propto 1/m_a \rightarrow$ the only unknown

$$a = \langle a \rangle + a_{phy} \rightarrow \frac{g^2}{32\pi^2} \frac{a_{phy}}{f_a} G_a^{\mu\nu} \tilde{G}_{\mu\nu a} \text{ which is CP even with pseudoscalar axion field}$$

Axion advent as a natural solution of the Strong CP problem in the SM

Axion models : KSVZ vs. DFSZ, invisible axion models



Prof. Jhin E. Kim,
inventor of
invisible axion

Axion production : Misalignment mechanism

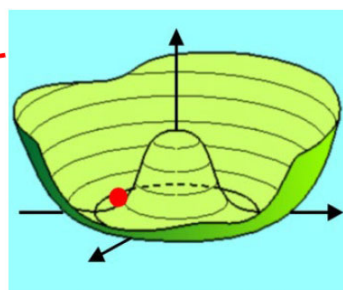
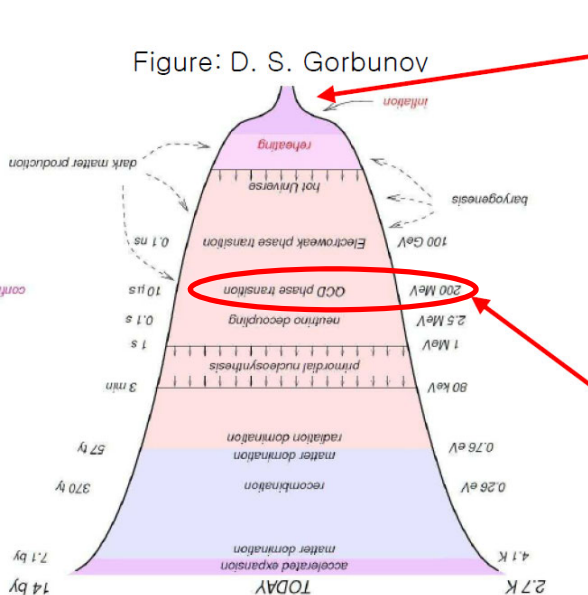
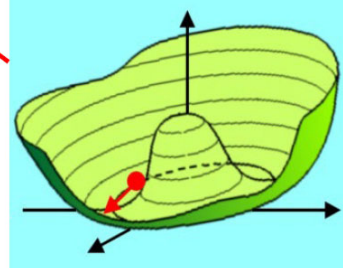


Figure: G. Raffelt



- axion produced with PQ symmetry breaking before the inflation
- axion at θ_{SM} w.r.t. the minimum → called **misalignment production**
- potential tilted by QCD → axion rolls down and starts small coherent oscillation around the minimum → the oscillation energy makes up a sizeable fraction of the energy density of our Universe

Axion born as cold

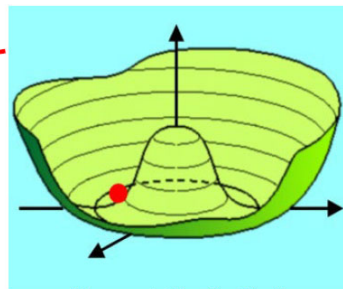
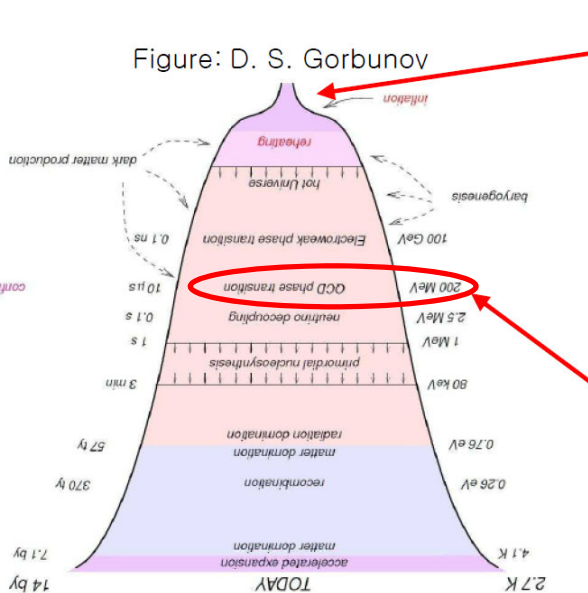
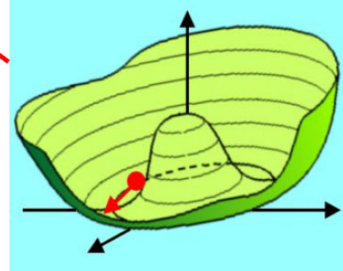


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• small oscillation → $\vec{\nabla} a \approx 0 \rightarrow \vec{p}a \approx 0 \rightarrow$ non-relativistic → **cold**

• axion energy, $E_a = m_a c^2 + \frac{1}{2} m_a v^2 = m_a c^2 \left(1 + \frac{1}{2} \left(\frac{v}{c} \right)^2 \right)$

Axion as cold dark matter

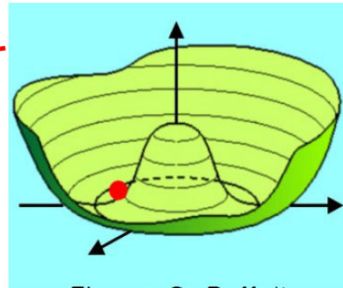
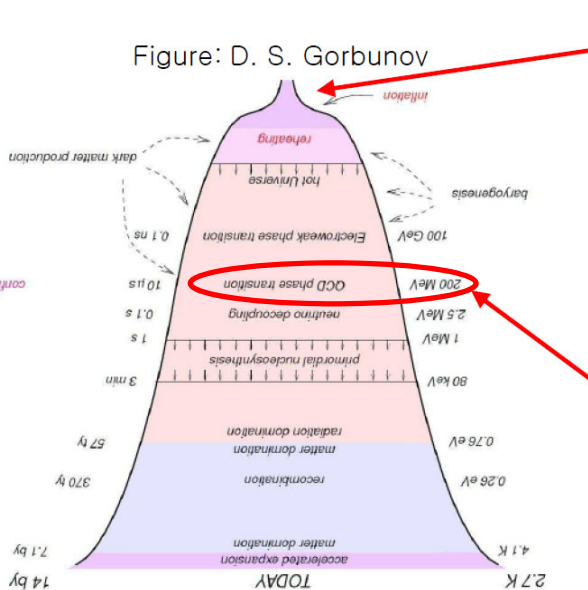
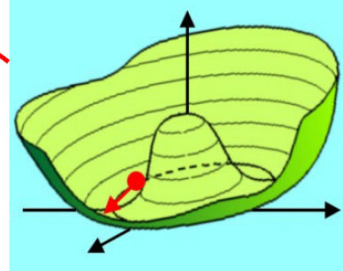


Figure: G. Raffelt

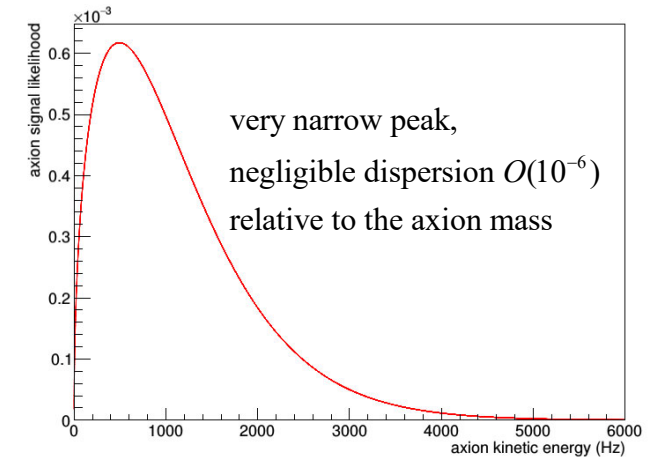


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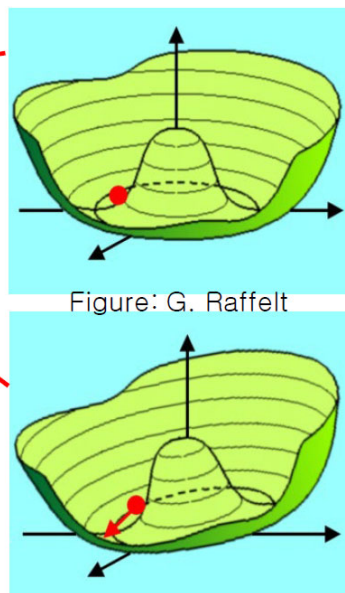
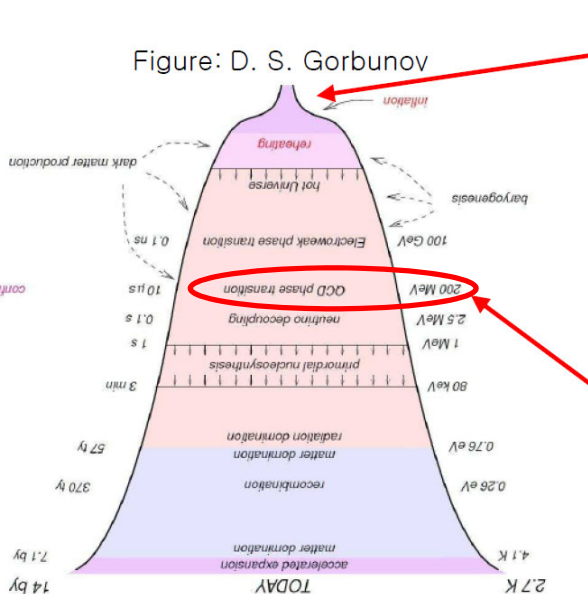
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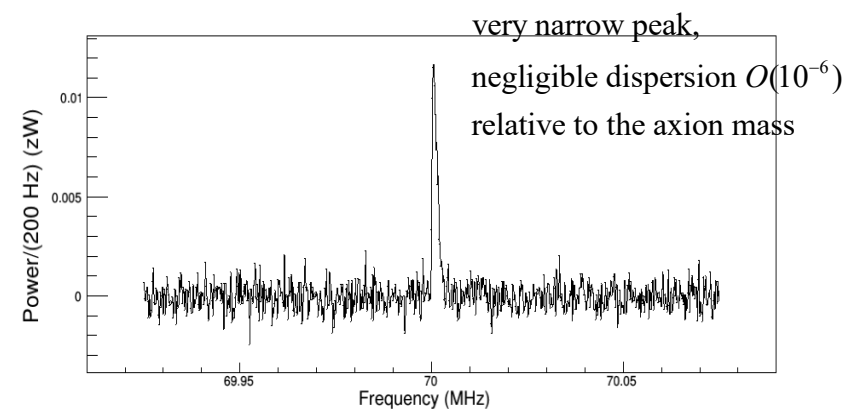
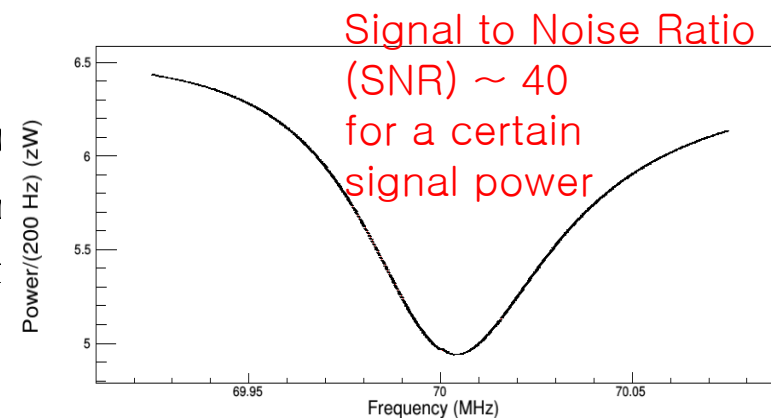
• using the standard halo model, $v^2/c^2 \sim O(10^{-6})$ and the v distribution follows the Maxwell-Boltzmann



Axion as cold dark matter



- axion produced with PQ symmetry breaking before the inflation
- axion at θ_{SM} w.r.t. the minimum \rightarrow called **misalignment production**
- potential tilted by QCD
oscillation around the minimum
a sizeable fraction of



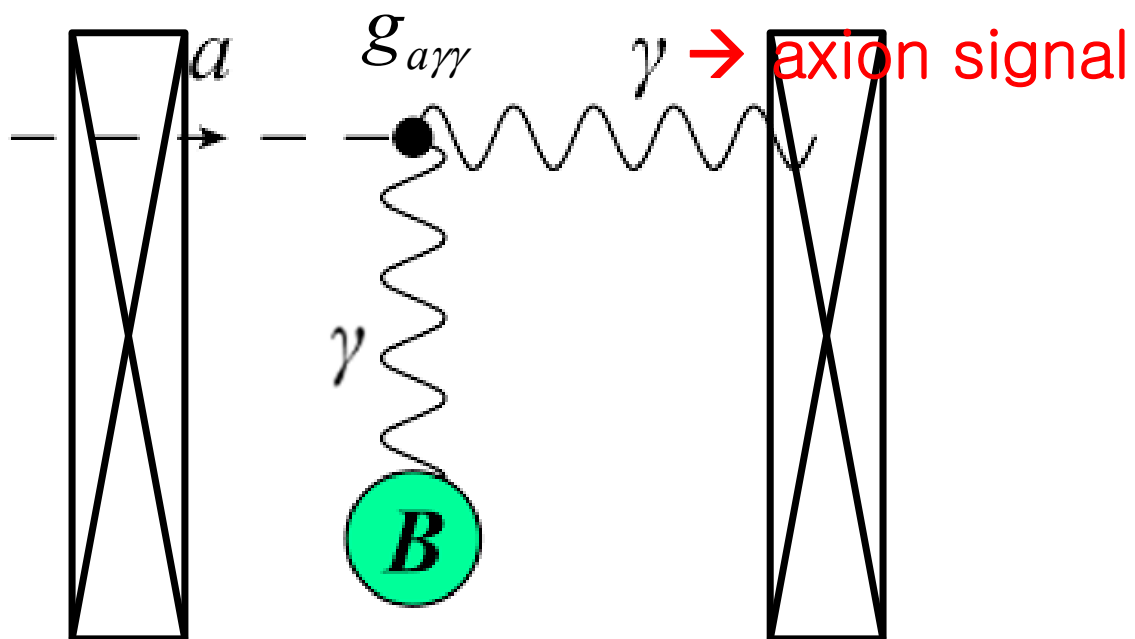
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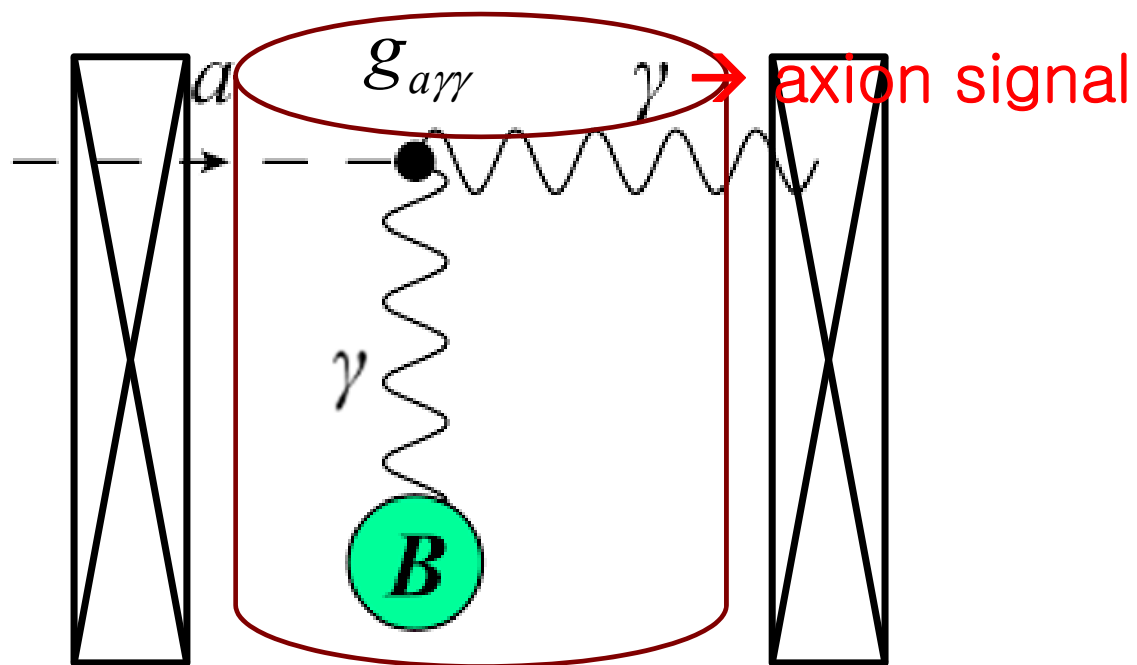
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Axion detection

- use axion-photon conversion
@ B-field



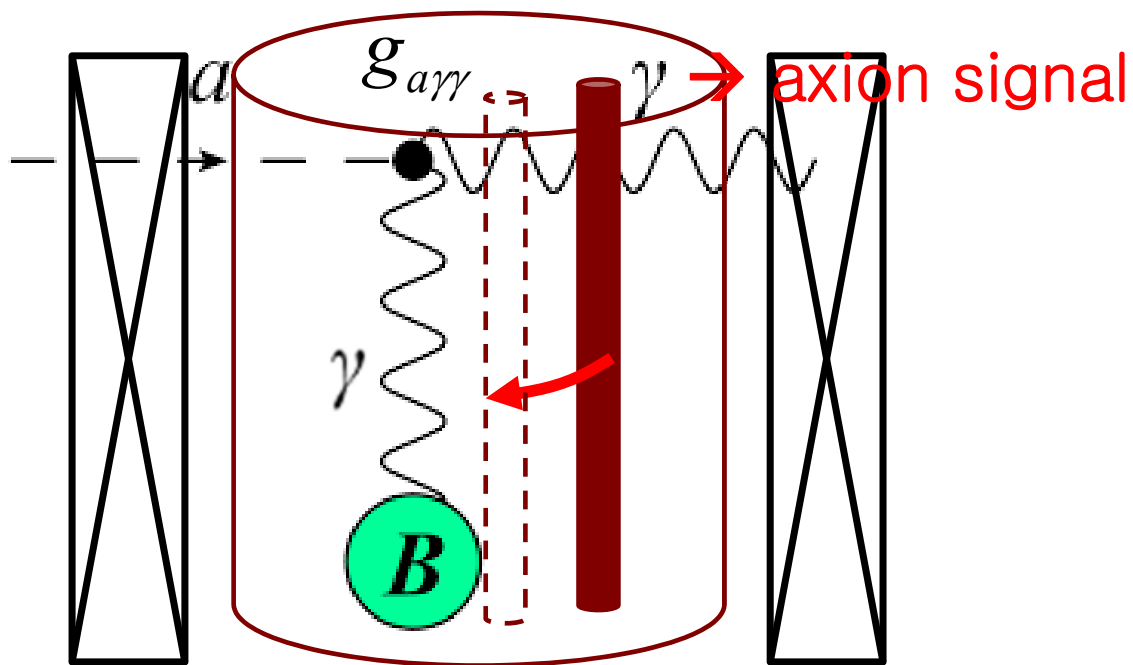
Axion detection



- use axion-photon conversion
@ B-field
- resonant conversion with a cavity

Axion detection

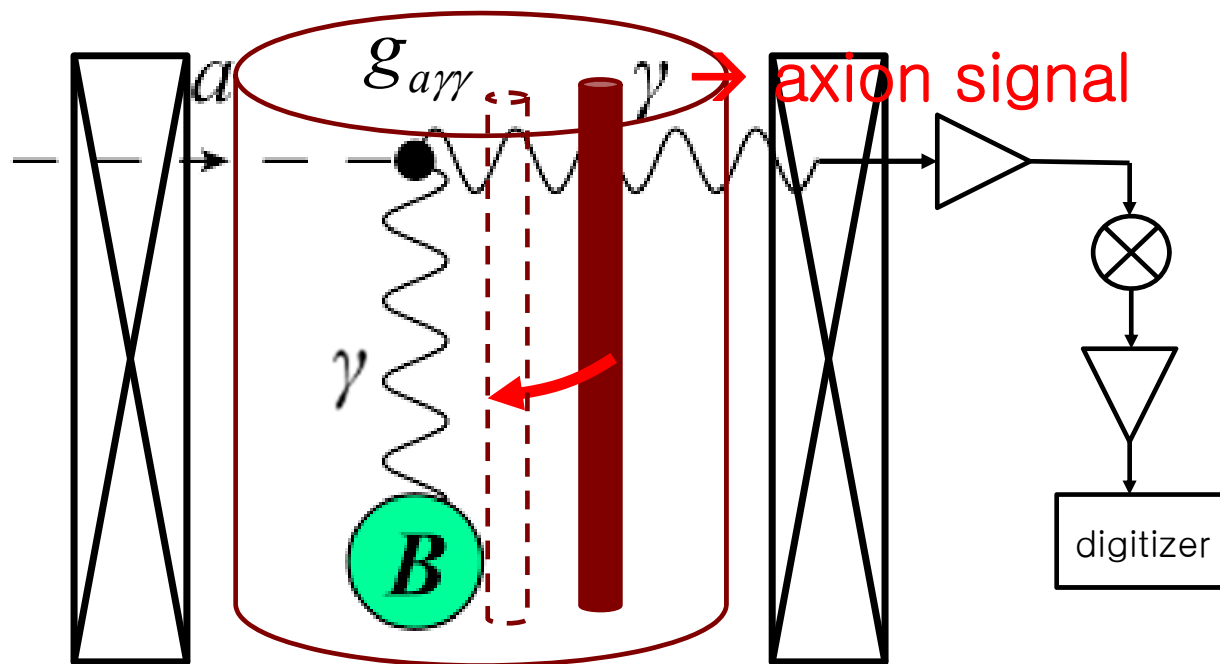
$$\bullet P_a^{a\gamma\gamma} \propto g_{a\gamma\gamma}^2 B^2 V \omega_{TM_{010}} Q_{cavity} a^2 / \mu_0$$



- use axion-photon conversion @ B-field
- resonant conversion with a cavity
- frequency tuning with a tuning rod due to unknown axion mass and the resonant conversion

Axion detection

$$\bullet P_a^{a\gamma\gamma} \propto g_{a\gamma\gamma}^2 B^2 V \omega_{TM_{010}} Q_{cavity} a^2 / \mu_0$$

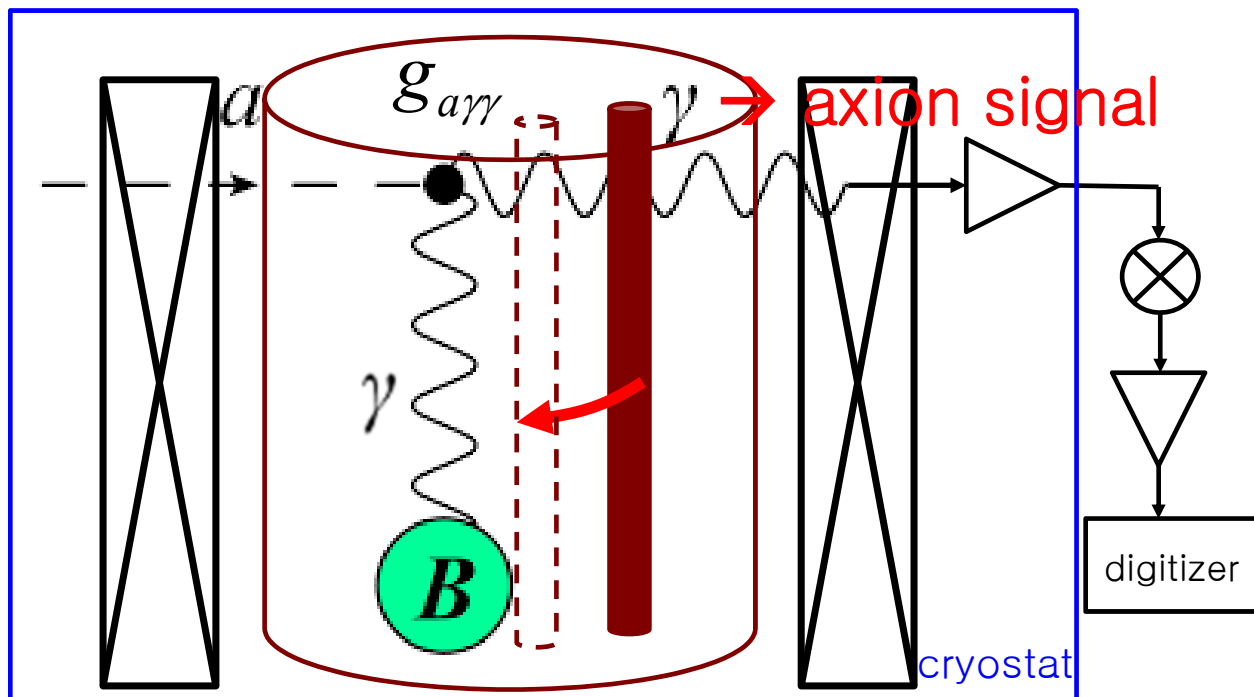


- use axion-photon conversion @ B-field
- resonant conversion with a cavity
- frequency tuning with a tuning rod due to unknown axion mass and the resonant conversion
- typical heterodyne receiver
- signal processing with a fast digitizer

Axion detection

$$\bullet P_a^{a\gamma\gamma} \propto g_{a\gamma\gamma}^2 B^2 V \omega_{TM_{010}} Q_{cavity} a^2 / \mu_0 \Rightarrow SNR = \frac{P_a^{a\gamma\gamma}}{\sigma_{P_{noise}}}$$

$$P_{noise} = k_B \Delta f T_{sys}, \quad T_{sys} = T_{cavity} + T_{chain}$$



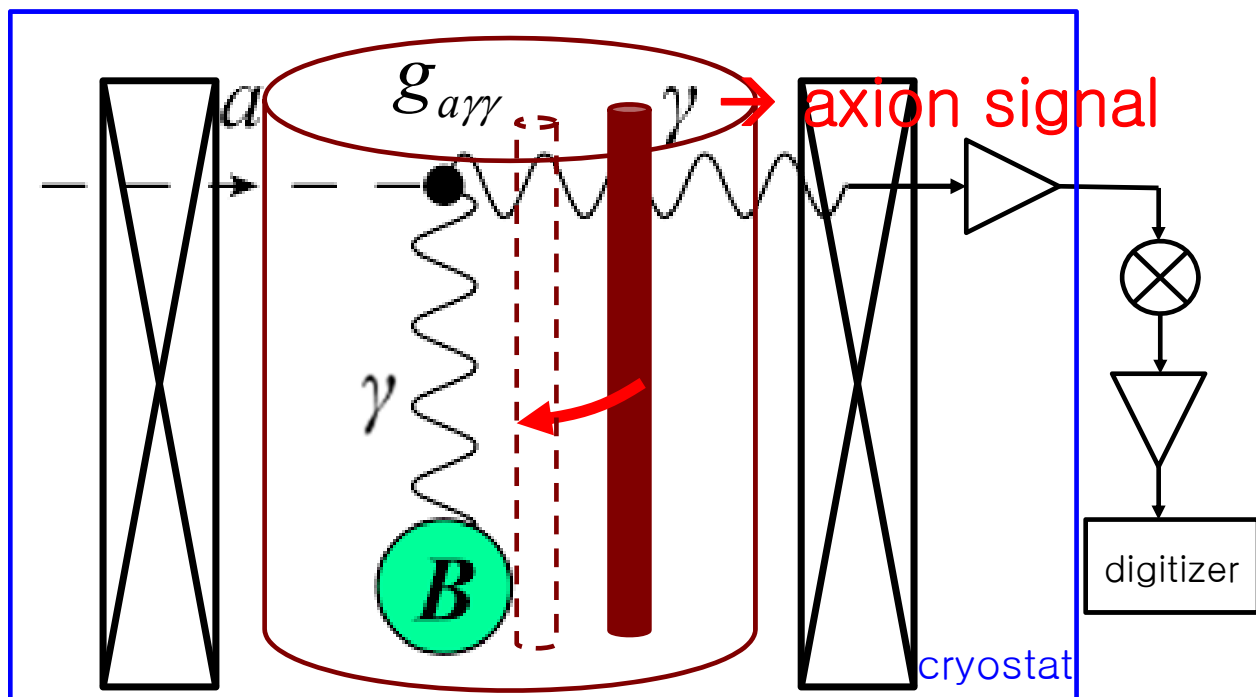
- use axion-photon conversion @ B-field
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Axion detection

$$\bullet P_a^{a\gamma\gamma} \propto g_{a\gamma\gamma}^2 B^2 V \omega_{TM_{010}} Q_{cavity} a^2 / \mu_0$$

$$P_{noise} = k_B \Delta f T_{sys}, \quad T_{sys} = T_{cavity} + T_{chain}$$

$$\Rightarrow \text{scanning rate } \frac{dv_{TM_{010}}}{dt} \propto \frac{g_{a\gamma\gamma}^4 B^4 V^2 Q_{cavity} a^4}{T_{noise}^2} \rightarrow \text{Figure of merit}$$



- use axion-photon conversion @ B-field
- resonant conversion with a cavity
- frequency tuning with a tuning rod due to **unknown axion mass and the resonant conversion**
- typical heterodyne receiver
- signal processing with a fast digitizer
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Axion dark matter detection

$$\bullet P_a^{a\gamma\gamma} \propto g_{a\gamma\gamma}^2 B^2 V \omega_{TM_{010}} Q_{cavity} a^2 / \mu_0$$

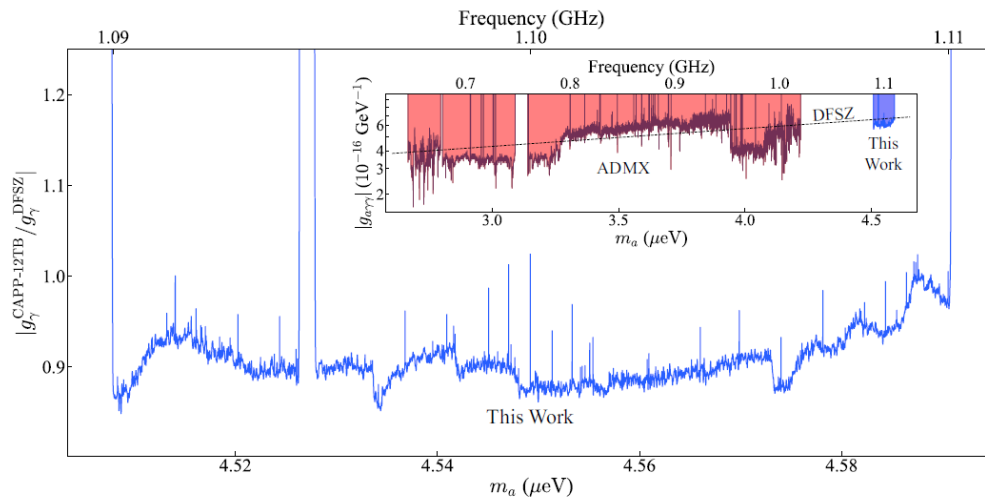
$$[a^2] = \frac{\text{kg}}{\text{s}} \rightarrow a^2 = \frac{\rho_a \hbar^2}{m_a^2 c} \text{ in SI units,}$$

ρ_a (local dark matter density) = 0.3 ~ 0.45 GeV/cc in natural units

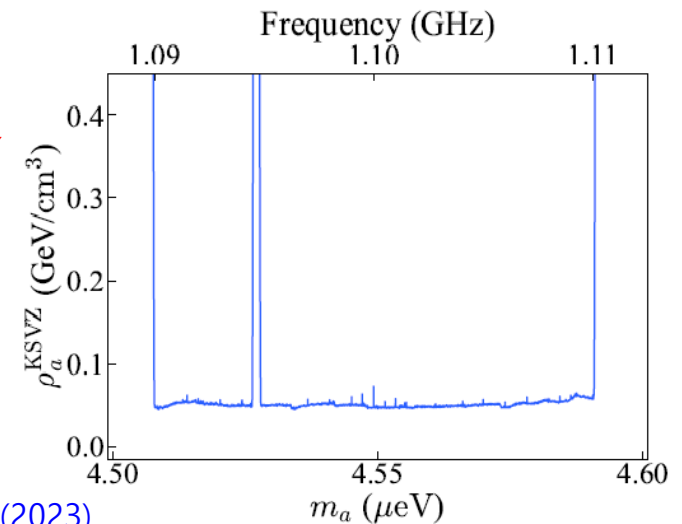
$$P_a^{a\gamma\gamma} \propto g_{a\gamma\gamma}^2 B^2 V \omega_{TM_{010}} Q_{cavity} \frac{\rho_a}{m_a^2} \rightarrow \text{axion signal depends on the local dark matter density } \rho_a \text{ as well as } g_{a\gamma\gamma}$$

for a
given ρ_a ,

$$g_{a\gamma\gamma} = \frac{\alpha g_\gamma}{\pi f_a}$$



for a
given $g_{a\gamma\gamma}^{KSVZ}$



PRL **130**,071002 (2023)

Axion experiment at IBS-CAPP—pushing the experimental parameters to extreme Magnet

•scanning rate $\frac{dv_{TM_{010}}}{dt} \propto \frac{B^4 V^2 Q_{cavity}}{T_{noise}^2} \rightarrow \text{Figure of merit}$

Superconductor magnet from Oxford Instruments (OI)



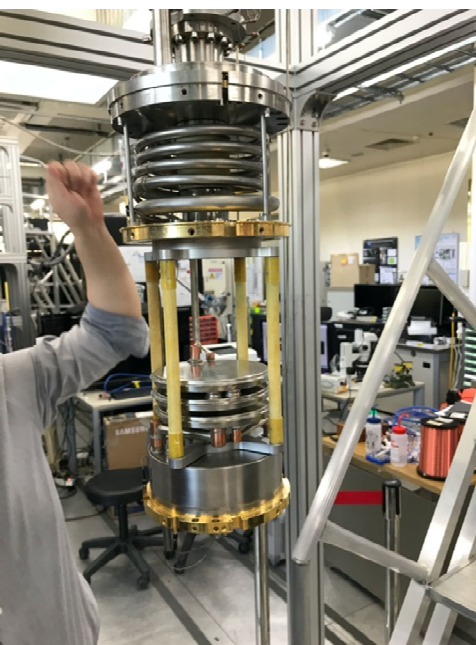
Magnet parameters	Values
Central field	12 T@4.2 K
Magnet bore	320 mm
Operating current	266 A
Inductance	161 H
Stored energy	5.7 MJ

300,000 times stronger than the
geomagnetic field there
→ $\sim 8 \times 10^{21}$ for the scanning rate

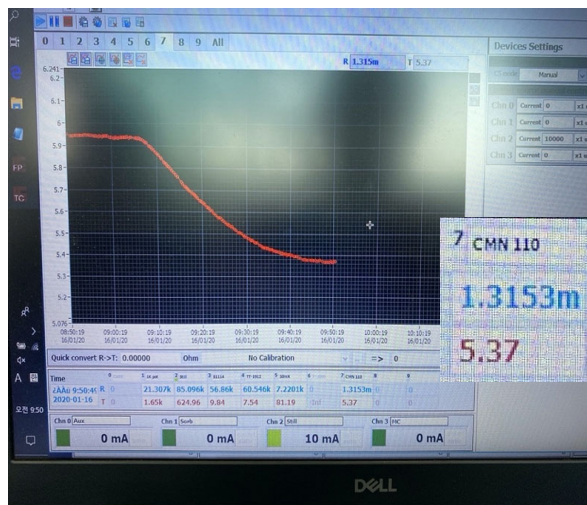
Axion experiment at IBS-CAPP—pushing the experimental parameters to extreme Fridge

• scanning rate $\frac{dv_{TM_{010}}}{dt} \propto \frac{B^4 V^2 Q_{cavity}}{T_{noise}^2} \rightarrow \text{Figure of merit}$ $T_{noise} = T_{cavity} + T_{chain}$

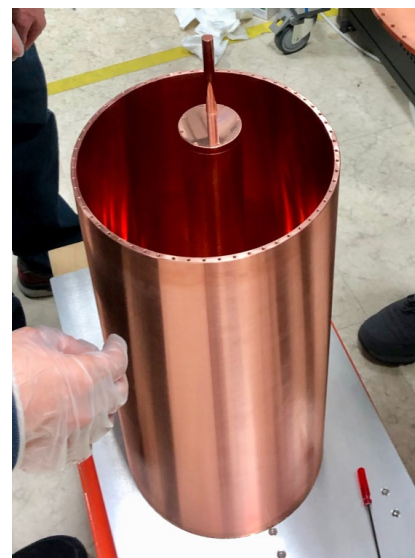
Dilution fridge from Leiden Cryogenic B.V.



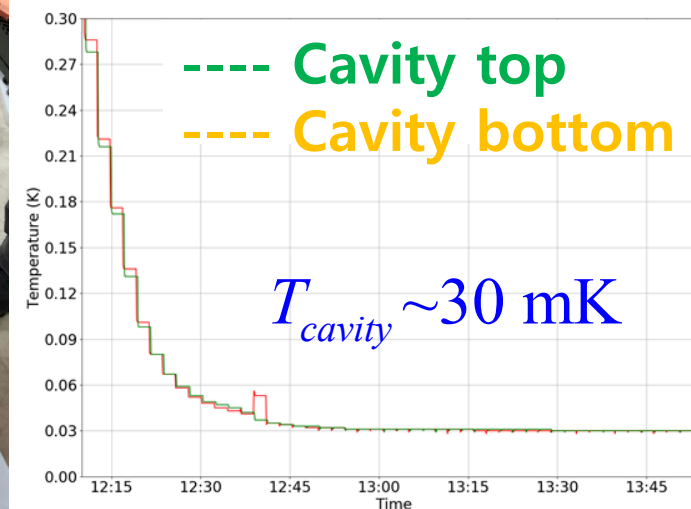
dilution insert unit



- base temperature 5.4 mK without load
- cooling power measured to be 1 mW at 90 mK



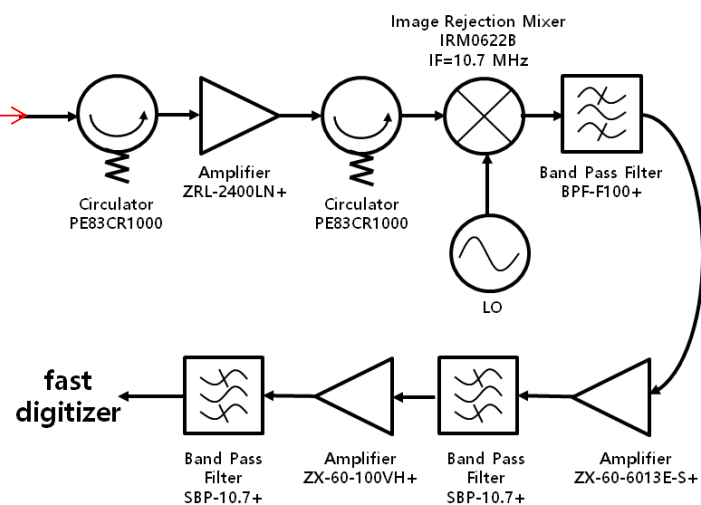
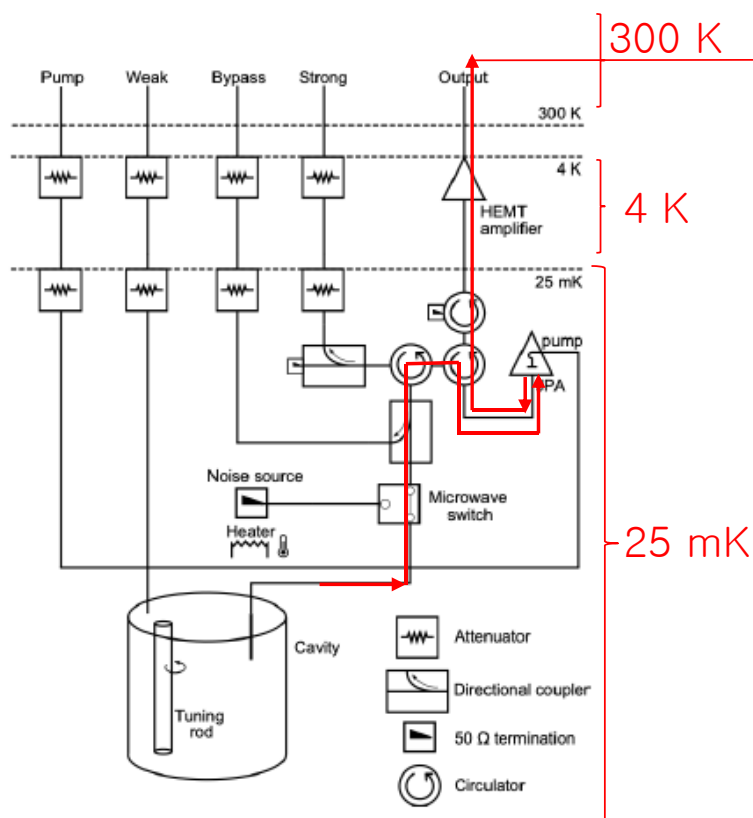
~55 kg



Axion experiment at IBS-CAPP—pushing the experimental parameters to extreme

Readout electronics

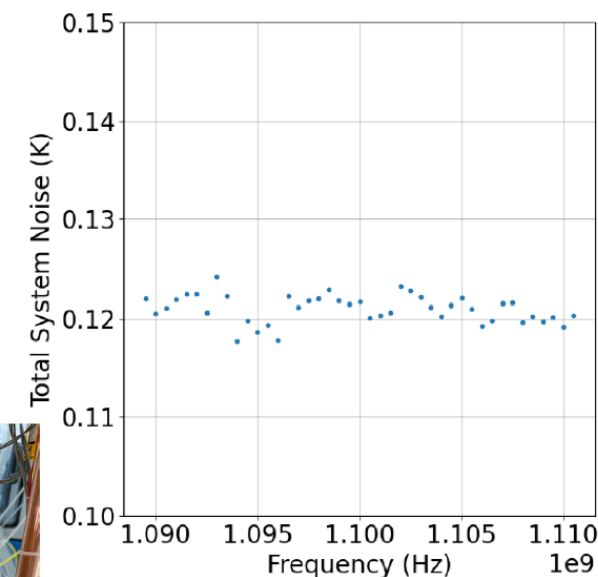
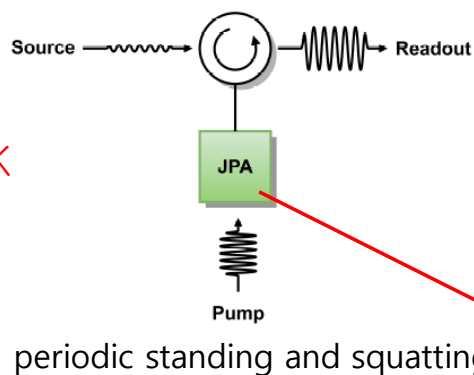
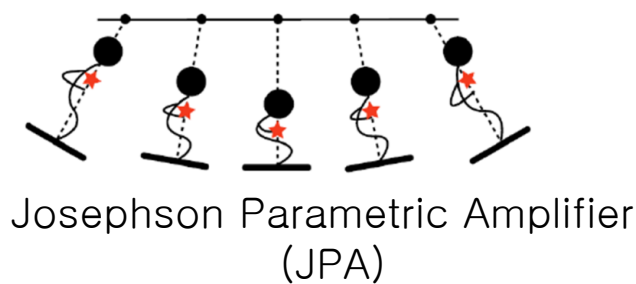
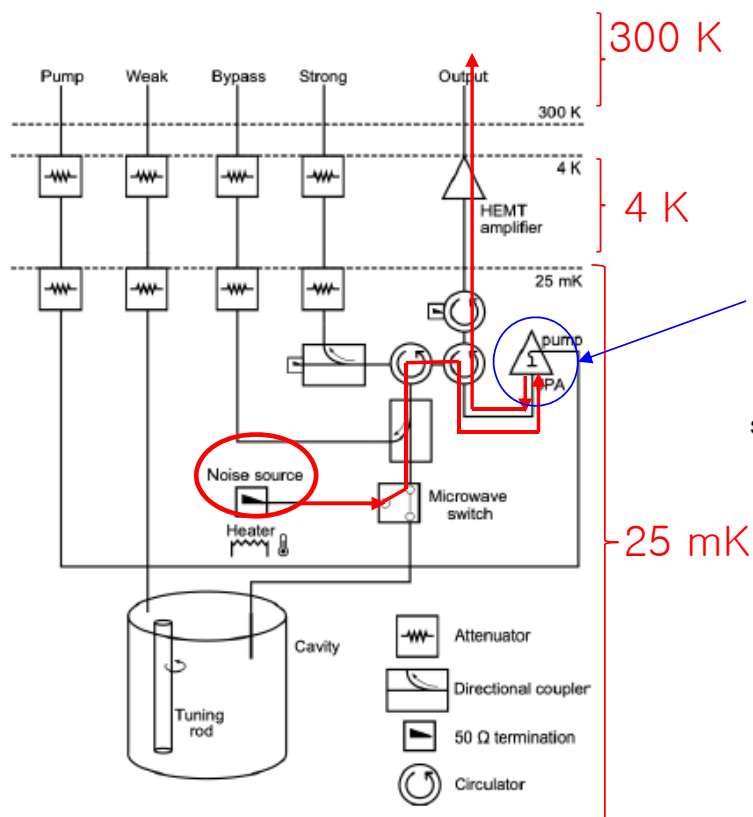
•scanning rate $\frac{dv_{TM_{010}}}{dt} \propto \frac{B^4 V^2 Q_{cavity}}{T_{noise}^2} \rightarrow$ Figure of merit $T_{noise} = T_{cavity} + T_{chain}$



Axion experiment at IBS-CAPP—pushing the experimental parameters to extreme

Readout electronics

•scanning rate $\frac{dv_{TM_{010}}}{dt} \propto \frac{B^4 V^2 Q_{cavity}}{T_{noise}^2} \rightarrow \text{Figure of merit}$ $T_{noise} = T_{cavity} + T_{chain}$

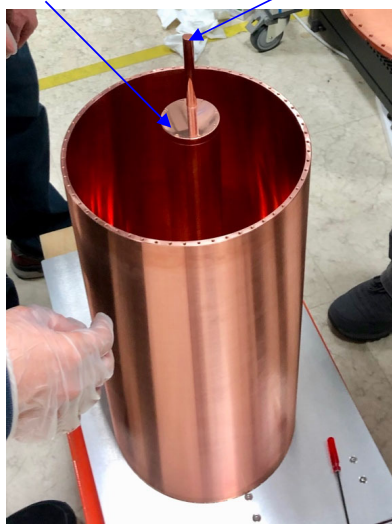


Axion experiment at IBS-CAPP—pushing the experimental parameters to extreme

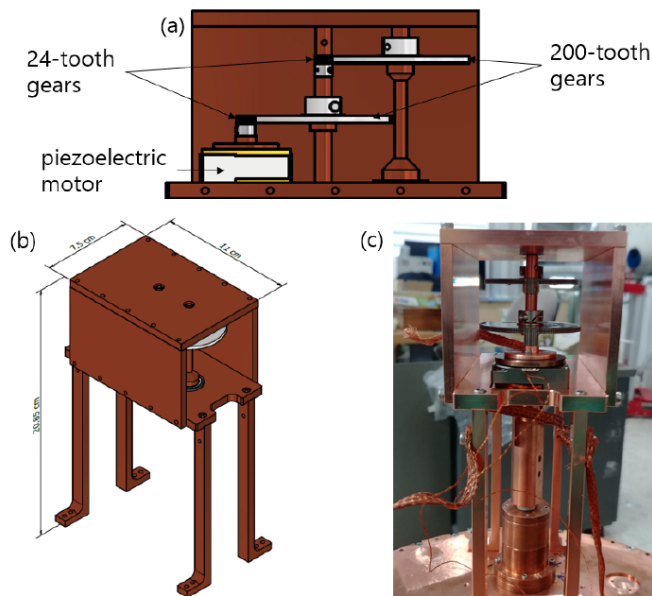
Tunable microwave cavity

•scanning rate $\frac{dv_{TM_{010}}}{dt} \propto \frac{B^4 V^2 Q_{cavity}}{T_{noise}^2} \rightarrow$ Figure of merit

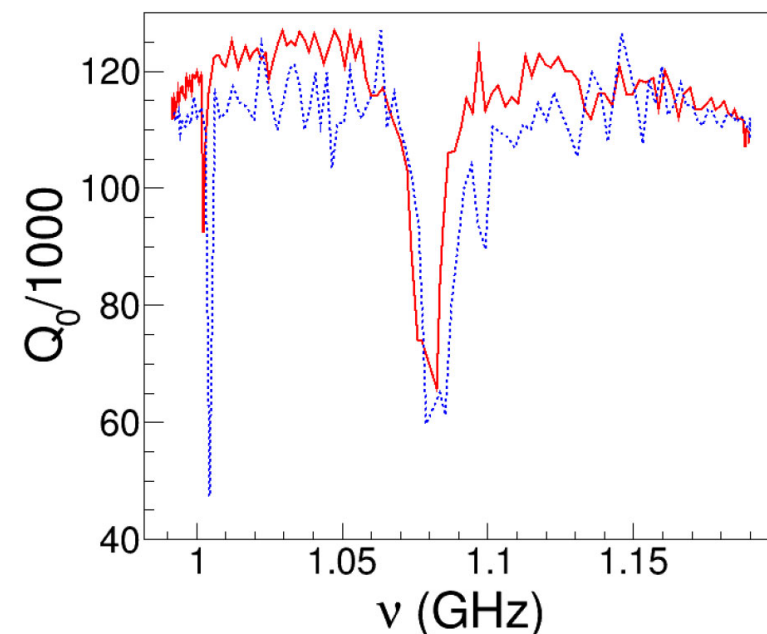
tuning rod tuning axle



OFHC copper
ID=262 mm, h=560 mm
tunable TM_{010} using
the tuning rod (OD=64 mm)
1.0~1.2 GHz



tuning mechanism by
piezo and gear combination
reduction ratio 69.4:1



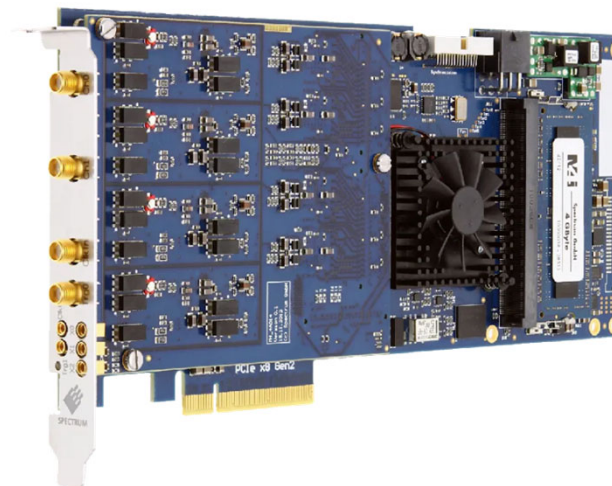
Q measurement at ~4 K

Axion experiment at IBS-CAPP—pushing the experimental parameters to extreme fast DAQ

- scanning rate $\frac{dv_{TM_{010}}}{dt} \propto \epsilon_{DAQ} \frac{B^4 V^2 Q_{cavity}}{T_{noise}^2} \rightarrow \text{Figure of merit}$



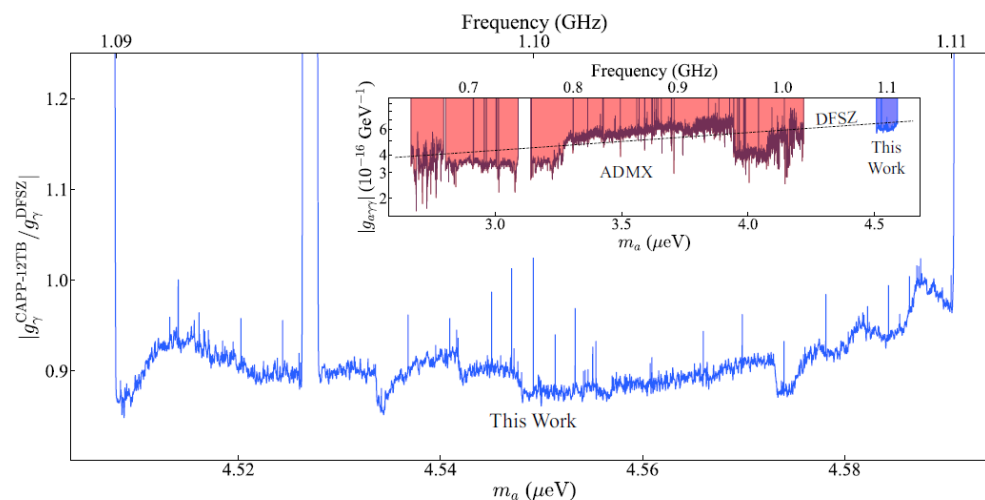
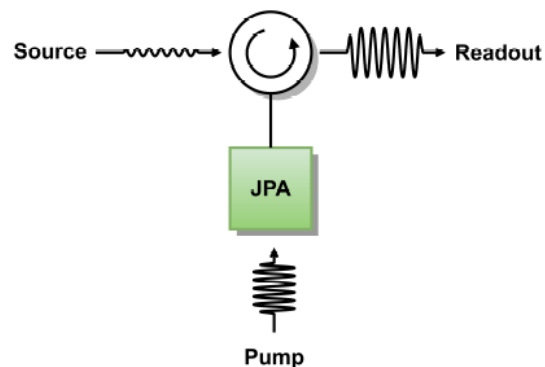
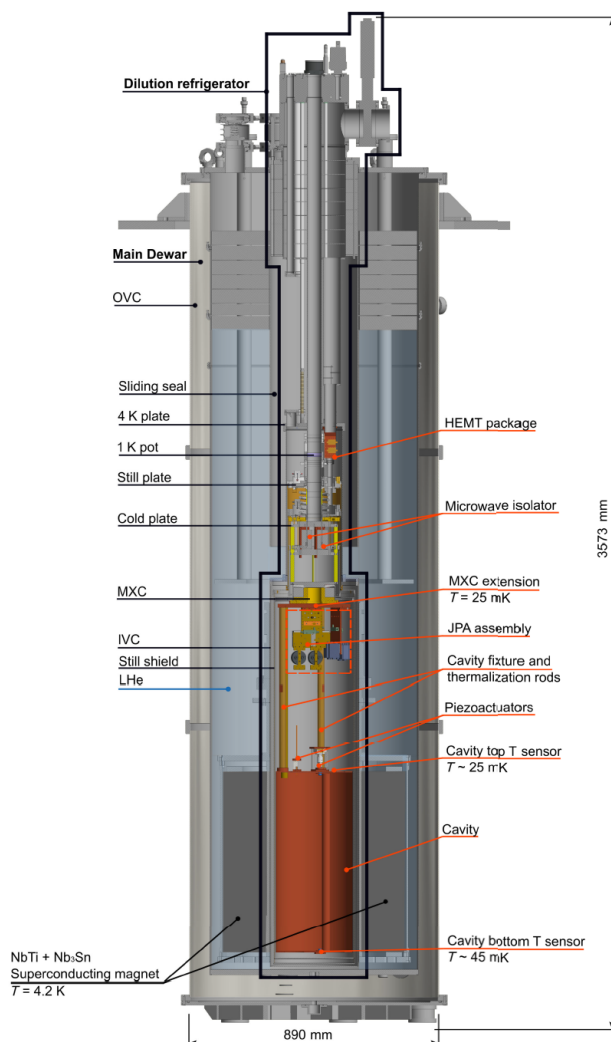
commercial spectrum analyzer
provides online FFT \rightarrow easy to use
DAQ efficiency at best $\sim 47\%$



using a fast digitizer,
developed a novel algorithm for online FFT
 \rightarrow realized a DAQ efficiency of $\sim 100\%$
(2022 JINST 17 P05025)

This is huge because you can finish your
experiment twice faster.

Axion experiment at IBS-CAPP—pushing the experimental parameters to extreme put it together

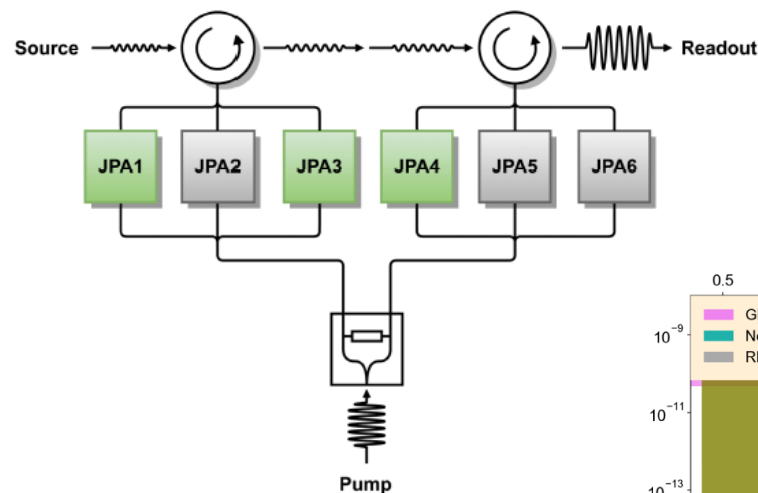
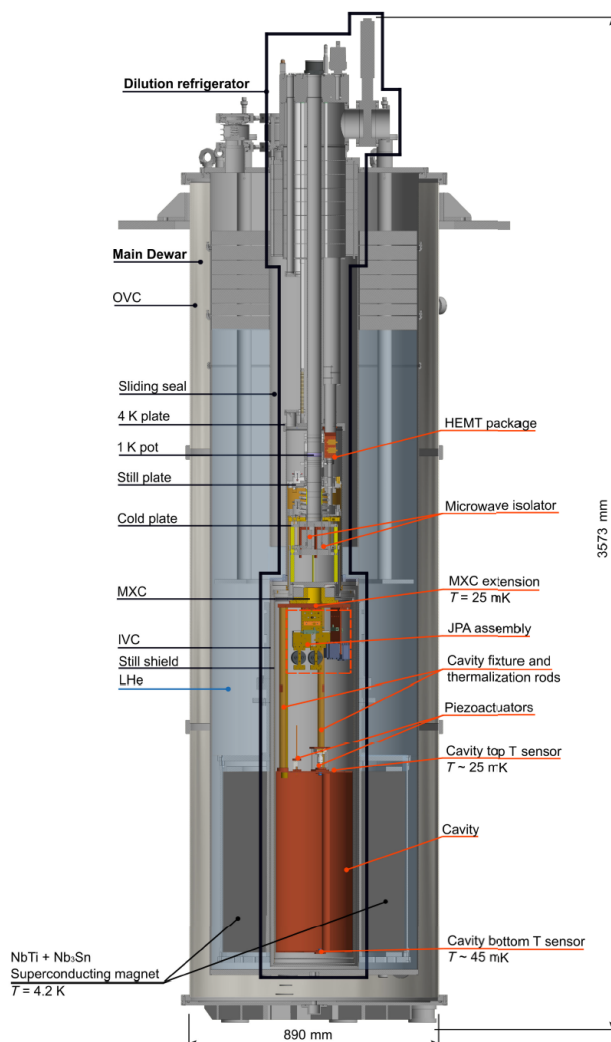


PRL **130**, 071002 (2023),
assuming axions make up 100% of the local dark matter density

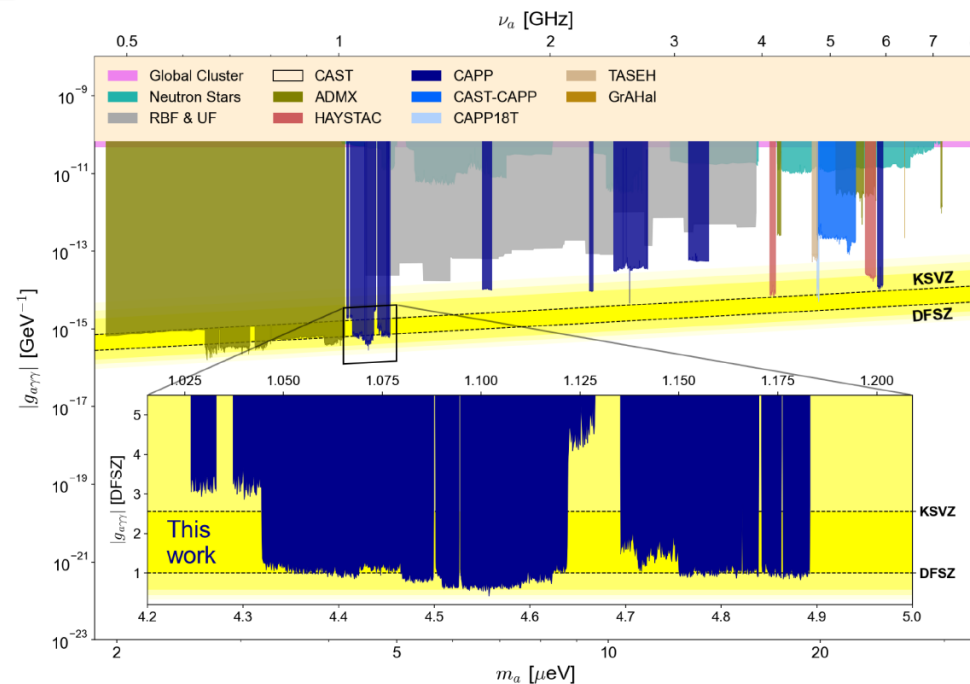
Scan 20 MHz in 18 days
Rate > 1 MHz/day maintaining
DFSZ sensitivity
→ best scanning rate ever

2nd experiment sensitive to
DFSZ axions
followed by ADMX (Axion Dark
Matter eXperiment) at
U. of Washington

Axion experiment at IBS-CAPP—pushing the experimental parameters to extreme put it together

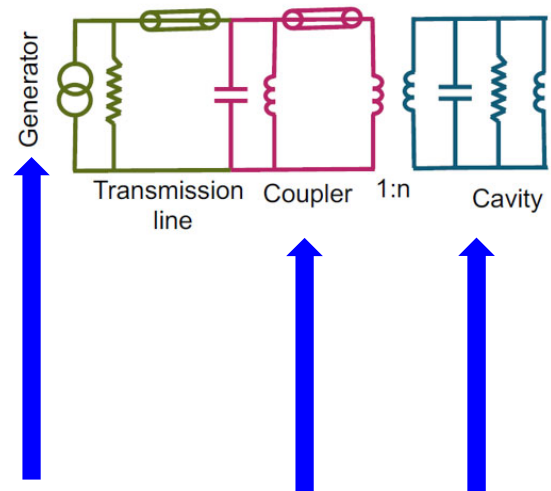
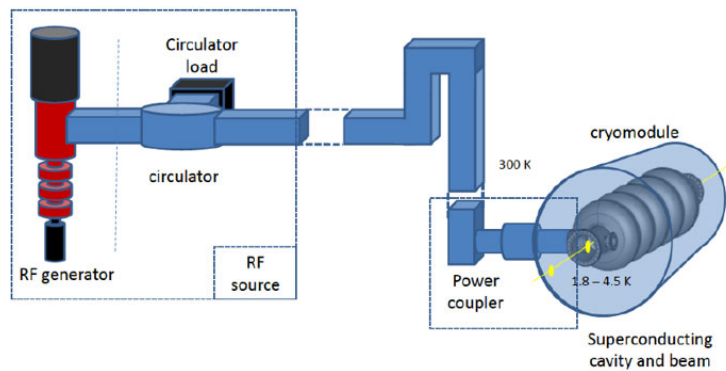


Scan > 100 MHz
Very non-trivial



PRX **14**, 031023 (2024),
assuming axions make up 100% of the local dark matter density

Summary



axion dark
matter halo

$g_{a\gamma\gamma}$

cavity
mode

$E_a^{\alpha\gamma\gamma}$

accelerating gradient

$$E_{acc} \propto \sqrt{Q_{cavity}}$$

axion signal power


















$$P_a^{a\gamma\gamma} \propto Q_{cavity}$$

$$\rightarrow E_a^{a\gamma\gamma} \propto \sqrt{Q_{cavity}}$$

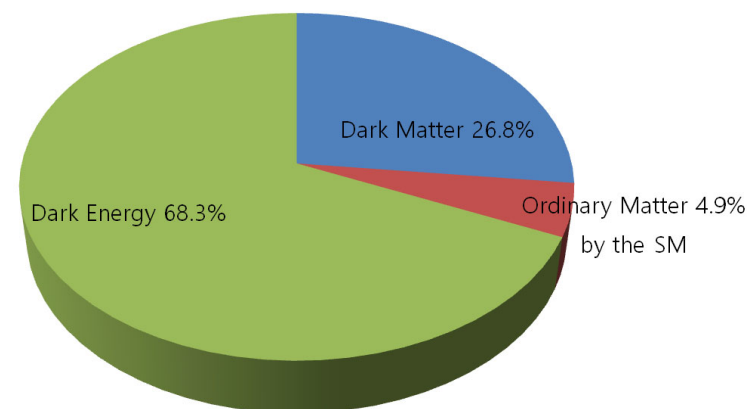
$$\text{if } m_a = \nu_{cavity}$$



Summary



















QUARKS	mass: 2.2* charge: 2/3 spin: 1/2  u up	1,270 2/3 1/2  c charm	173,100 2/3 1/2  t top	BOSONS	0 0 1  g gluon	125,180 0 0  H Higgs boson
	4.7 -1/3 1/2  d down	96 -1/3 1/2  s strange	4,180 -1/3 1/2  b bottom		0 0 1  γ photon	
	0.511 -1 1/2  e electron	105.66 -1 1/2  μ muon	1,776.8 -1 1/2  τ tau		91,188 0 1  Z Z boson	
LEPTONS	<0.00000012 0 1/2  ν _e electron neutrino	<0.00000012 0 1/2  ν _μ muon neutrino	<0.00000012 0 1/2  ν _τ tau neutrino		80,379 +/-1 1  W W boson	

Energy budget of the Universe

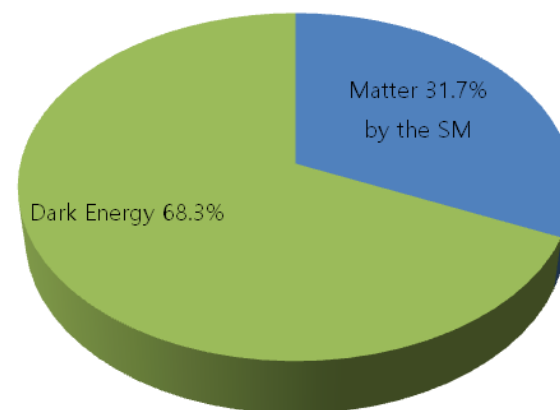


- SM governs ~5% of the Universe

Summary

QUARKS	mass: 2.2^* charge: $2/3$ spin: $1/2$  up	1,270 $2/3$ $1/2$  charm	173,100 $2/3$ $1/2$  top	BOSONS	0 0 1  gluon	125,180 0 0  Higgs boson
	4.7 $-1/3$ $1/2$  down	96 $-1/3$ $1/2$  strange	4,180 $-1/3$ $1/2$  bottom		0 0 1  photon	
	0.511 -1 $1/2$  electron	105.66 -1 $1/2$  muon	1,776.8 -1 $1/2$  tau		91,188 0 1  Z boson	
LEPTONS	<0.00000012 0 $1/2$  electron neutrino	<0.00000012 0 $1/2$  muon neutrino	<0.00000012 0 $1/2$  tau neutrino		80,379 ± 1 1  W boson	? 0 0  axion

Energy budget of the Universe



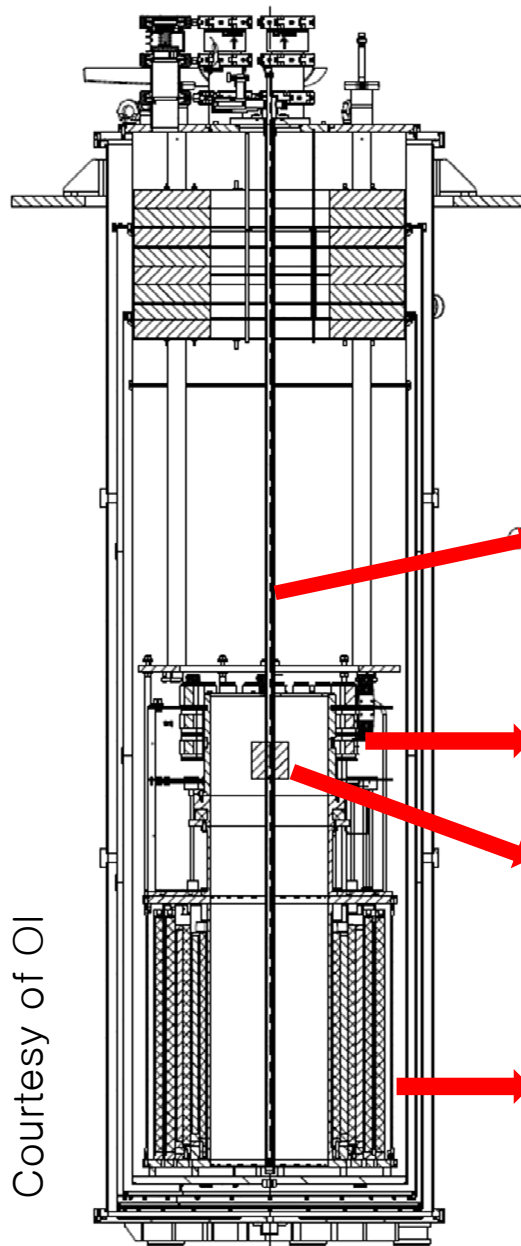
- We govern all matter (~32% of the Universe) together with axion dark matter
→ promotion of the SM ?

Dark Matter Candidates

	Axions	WIMPs
Year invented	1977	1985
Original purpose	Solve technical problem in theory of strong nuclear force	Explain dark matter
Detectable because they	Turn into photons in strong magnetic fields	Bounce off atomic nuclei
Pros	Solve more than one problem; allow for decisive test	Flow naturally from supersymmetry; provide many models and multiple avenues of detection
Cons	Provide few models and one means of detection	Resist decisive testing; haven't shown up in decades of looking

Science, Vol 342, 1 Nov. 2013

Magnet details



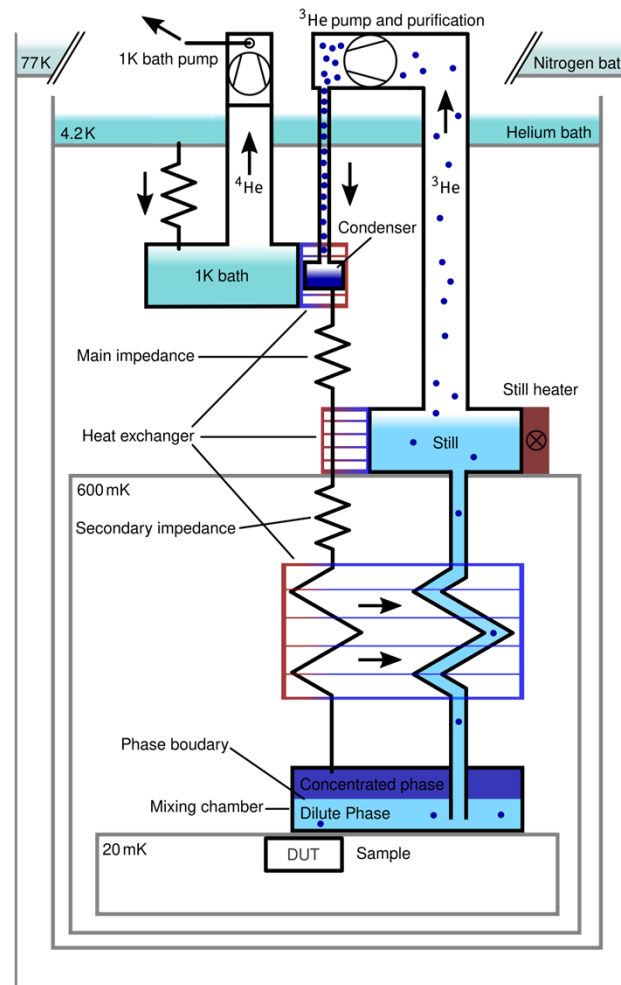
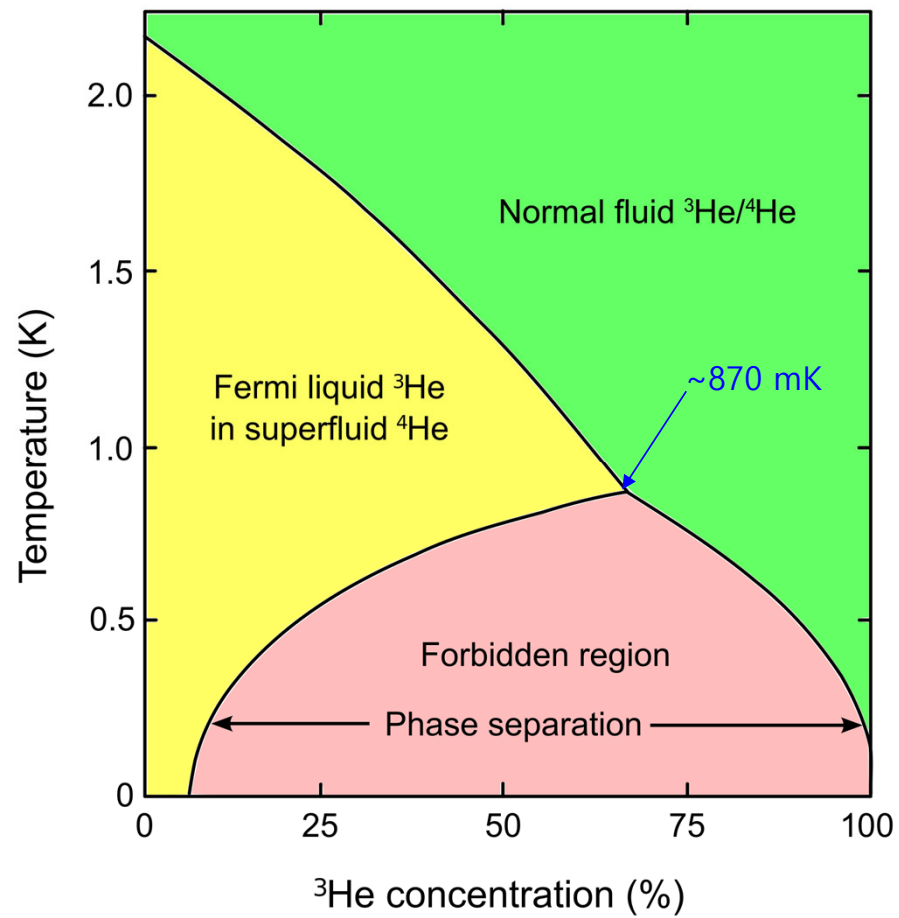
Courtesy of OI

Hall probes for the factory test

cancellation coil : NbTi only

cancellation region : <100 G
over 100 mm (D) x100 mm (h)

main coil : nested coils
with Nb₃Sn (600mm, inner) and
NbTi (800mm, outer)



^3He is diluted from the concentrated phase to the diluted phase through the phase boundary

Haus-Caves theorem

$$V(t) = V_0 \left(\hat{X}_1(t) \cos \omega_0 t + \hat{X}_2(t) \sin \omega_0 t \right)$$

$$\text{quadratures } \hat{X}_1 = \frac{1}{2}(\hat{a} + \hat{a}^\dagger) \text{ and } \hat{X}_2 = \frac{1}{2}(\hat{a} - \hat{a}^\dagger)$$

$$[\hat{X}_1, \hat{X}_2] = \frac{i}{2} \text{ and } [\hat{a}, \hat{a}^\dagger] = 1$$

$$\hat{Y}_1 = \sqrt{G_1} \hat{X}_1 + \hat{F}_1$$

$$\hat{Y}_2 = \sqrt{G_2} \hat{X}_2 + \hat{F}_2$$

$$[\hat{F}_1, \hat{F}_2] = \frac{i}{2} (1 - \sqrt{G_1 G_2}) = \frac{i}{2} (1 - G)$$

$$A_N = \frac{1}{2} \left| 1 \mp \frac{1}{G} \right|$$

Axion quality problem

Quantum-gravity effects at the Planck scale
spoil the PQ solution to the strong CP problem